

Name: Key

Date: COPY Yellow  
Proof Reasons  
Sheet!

### Geometry Notes Into to Geo Proofs - 3: Definitions and Drawing Conclusions

#### Definitions (Review)

In math, a precise definition should work "both ways." (It is a biconditional.)

Ex: A triangle is a polygon with exactly three sides.

- 1. If a polygon is a triangle, then it has exactly three sides. True
  - 2. If a polygon has exactly three sides, then it's a triangle. True
- } Good Def of a  $\Delta$

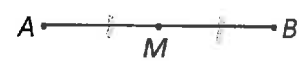
Ex: A square is a polygon with exactly four sides.

- 1. If a polygon is a square, then it has exactly four sides. True
  - 2. If a polygon has exactly four sides, then it's a square. false
- } Not a Good Def of a square
- \* parallelogram  
\* rhombus  
\* Trap

#### Drawing simple conclusions

We can use definitions to draw simple conclusions.

1. Given:  $M$  is the midpoint of  $\overline{AB}$ .

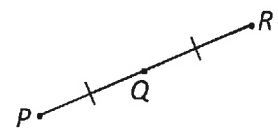


Conclusion:  $\overline{AM} \cong \overline{MB}$

Reason: A midpt cuts a segment into 2  $\cong$  segments

Note: Remember, in proofs, a "given" is assumed to be true.

2. Given:  $\overline{PQR}$  and  $\overline{PQ} \cong \overline{QR}$ .



Conclusion:  $Q$  is the midpoint of  $\overline{PR}$

Reason: The point that divides a segment into 2  $\cong$  segments is the midpt

3. Given:  $m\angle ABC + m\angle XYZ = 180^\circ$

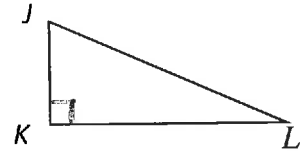
Conclusion:  $\angle ABC$  and  $\angle XYZ$  are supplementary

Reason: Supplementary  $\angle$ s add to  $180^\circ$

4. Given:  $\angle JKL$  is a right angle.

Conclusion:  $\angle K$  is a right  $\angle$

Reason: Same angle



Conclusion:  $\triangle JKL$  is a right  $\triangle$

Reason: A  $\triangle$  with a right  $\angle$  is a right  $\triangle$

Conclusion:  $\overline{JK} \perp \overline{KL}$

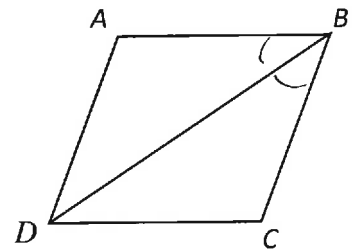
Reason:

Perpendicular lines meet to form right  $\angle$ s

5. Given:  $\overline{BD}$  bisects  $\angle ABC$

Conclusion:  $\angle ABC \cong \angle DBC$

Reason: A bisector cuts an  $\angle$  into 2  $\cong$  angles



Not:

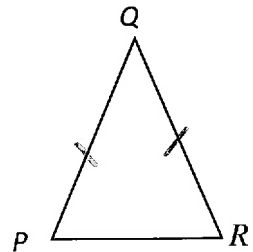
Not:

} When you bisect an  $\angle$  you get 2 new  $\angle$ s not segments

6. Given:  $\overline{PQ} \cong \overline{QR}$

Conclusion:  $\triangle PQR$  is isosceles

Reason:  $\triangle$  w/ 2  $\cong$  sides is isosceles



Name \_\_\_\_\_

$\angle P \cong \angle R \rightarrow$  angles opp  $\cong$  sides are  $\cong$